

Z Score Normalization

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<https://t4tutorials.com/z-score-normalization-data-mining/>

Z Score Normalization

Z-Score Normalization – (Data Mining)

Z-Score helps in the normalization of data. If we normalize the data into a simpler form with the help of z score normalization, then it's very easy to understand by our brains.

Z- Score Formula

$$Z = \frac{\text{Score} - \text{Mean}}{\text{SD}}$$

x μ σ SD

Z-Score Formula

The diagram illustrates the Z-score formula. The numerator consists of 'Score' (labeled 'x') minus 'Mean' (labeled 'μ'). The denominator is 'SD' (labeled 'σ'). The entire formula is labeled 'Z-Score Formula'.

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Example

How to calculate Z-Score of the following data?

| marks |
|-------|
| 8 |
| 10 |
| 15 |
| 20 |

$$s = \sqrt{\frac{\sum(x - \bar{x})^2}{n}}$$

Standard deviation = $\sqrt{\frac{\sum(\text{every individual value of marks} - \text{mean of marks})^2}{n}}$

Mean of marks = $8 + 10 + 15 + 20 / 4 = 13.25$

$$= \sqrt{\frac{(8 - 13.25)^2 + (10 - 13.25)^2 + (15 - 13.25)^2 + (20 - 13.25)^2}{4}}$$

$$= \sqrt{\frac{(-5.25)^2 + (-3.25)^2 + (1.75)^2 + (6.75)^2}{4}}$$

$$= \sqrt{\frac{27.56 + 10.56 + 3.06 + 45.56}{4}} = \sqrt{\frac{86.74}{4}} = \sqrt{21.6} = 4.6$$

$$ZScore = \frac{x - \mu}{\sigma} = \frac{8 - 13.25}{4.6} = -1.14$$

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$$ZScore = \frac{x - \mu}{\sigma} = \frac{10 - 13.25}{4.6} = -0.7$$

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$$ZScore = \frac{x - \mu}{\sigma} = \frac{15 - 13.25}{4.6} = 0.3$$

$$ZScore = \frac{x - \mu}{\sigma} = \frac{20 - 13.25}{4.6} = 1.4$$

| marks | marks after z-score normalization |
|--------------|-----------------------------------|
| 8 | -1.14 |
| 10 | -0.7 |
| 15 | 0.3 |
| 20 | 1.4 |

Download Excel File Calculations

| F63 | | | | | | | | | | |
|-----|------|---|-------|-------------|------|-----------------------------|------------|--------|----------|-----------|
| | A | B | C | D | E | F | G | H | I | J |
| 1 | | https://T4Tutorials.com | | | | | | | | |
| 2 | | | | | | after z-score normalization | | | | |
| 3 | Id | Depend | Sal | Euclidean | Id | Depend | Norm-Dep | Salary | Norm-Sal | Euclidean |
| 4 | E101 | 3 | 50000 | 0 | E101 | 3 | -0.5287788 | 50000 | 4.2954 | 0 |
| 5 | E105 | 5 | 50000 | 49999.37304 | E110 | 3 | -0.5287788 | 45000 | 3.86583 | 0.4295716 |
| 6 | E110 | 3 | 45000 | 5000 | E113 | 3 | -0.5287788 | 57000 | 4.8968 | 0.6014003 |
| 7 | E113 | 3 | 57000 | 7000 | E114 | 3 | -0.5287788 | 42000 | 3.60809 | 0.6873146 |
| 8 | E111 | 6 | 43000 | 7000.000643 | E112 | 4 | 0.293766 | 39000 | 3.35035 | 1.2528822 |
| 9 | E114 | 3 | 42000 | 8000 | E107 | 3 | -0.5287788 | 35000 | 3.00669 | 1.2887149 |
| 10 | E109 | 5 | 40000 | 10000.0002 | E108 | 4 | 0.293766 | 38000 | 3.26443 | 1.3188946 |
| 11 | E112 | 4 | 39000 | 11000.00005 | E102 | 4 | 0.293766 | 65000 | 5.58412 | 1.5288446 |
| 12 | E108 | 4 | 38000 | 12000.00004 | E104 | 4 | 0.293766 | 35000 | 3.00669 | 1.5288446 |
| 13 | E107 | 3 | 35000 | 15000 | E105 | 5 | 1.1163108 | 50000 | 4.2954 | 1.6450896 |
| 14 | E102 | 4 | 65000 | 15000.00003 | E103 | 3 | -0.5287788 | 70000 | 6.01369 | 1.7182865 |
| 15 | E104 | 4 | 35000 | 15000.00003 | E109 | 5 | 1.1163108 | 40000 | 3.43626 | 1.8559221 |
| 16 | E103 | 3 | 70000 | 20000 | E106 | 1 | -2.1738684 | 30000 | 2.57712 | 2.3788291 |
| 17 | E106 | 1 | 30000 | 20000.0001 | E111 | 6 | 1.9388556 | 43000 | 3.694 | 2.5398625 |

FAQ about Z Score Normalization

- **How do you use a z score table?**
- **Advantages of the z score**
- **Is a higher or lower Z score better?**
- **What does a negative and a positive z score mean?**
- **Why is the mean of Z scores is 0?**
- **What is the meaning of the high Z score and low Z score?**